Please provide details and steps of your work!!!

## Name:

## **Student ID or Lucky No.:**

- 1. (8 points) Let  $f(x) = x^{1/5}$ , find
  - (a) f'(x)
  - (b) the partition numbers for f'(x)
  - (c) the critical values of f(x).
- 2. (10 points) Let  $f(x) = x^3 12x + 12$  on the interval [-3, 5]. Identify the critical points and find the absolute maximum value and absolute minimum value on the given interval [-3, 5].
- 3. (16 points) Evaluate the following limits
  - (a)  $\lim_{x \to 0} \frac{e^{3x} 1}{x}$
  - (b)  $\lim_{x\to\infty} \frac{e^{3x}}{x^2}$
  - (c)  $\lim_{x\to 3} \frac{e^x e^3}{x 3}$
  - (d)  $\lim_{x \to 0} \frac{e^x 1 x}{x^2}$
- 4. (8 points) Use the second-derivative test to find any local extrema for

$$f(x) = x^3 - 6x^2 - 15x + 12$$

- 5. (10 points) Let  $f(x) = x^2(x-1) = x^3 x^2$ . Summarize all the pertinent information obtained by applying the graphing strategy to f, and then sketch the graph of f as follows.
  - (a) Analyze f(x): find the domain, intercepts, symmetry(if exists), asymptotes(if exists).
  - (b) Analyze f'(x): find local extrema, increasing and decreasing intervals.
  - (c) Analyze f''(x): find inflection points, concavity.
  - (d) Sketch the graph of f.
- 6. (15 points) Find each indefinite integral:
  - (a)  $\int 2dx$
  - (b)  $\int \left(\frac{3}{x} 4e^x\right) dx$
  - (c)  $\int (8\sqrt{x} \frac{6}{\sqrt{x}})dx$
  - (d)  $\int \frac{7}{4x+7} dx$
  - (e)  $\int \frac{(\ln x)^3}{x} dx$
- 7. (8 points) Find the particular antiderivative of the following derivative that satisfies the given initial condition:

$$F'(x) = 6x^2 - 4x; F(0) = 3$$

8. (8 points) Find the derivative or indefinite integral of the following:

(a) 
$$\frac{d}{dx} (\int e^{-x^2} dx)$$

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(b)  $\int \frac{d}{dx} (\sqrt{4+5x}) dx$ 

- 9. (5 points) Calculate the Riemann sum  $S_n = \sum_{i=1}^n f(c_i) \Delta x_i$  when f(x) = 2x; the partition is  $P_5: 0 < 0.5 < 1.25 < 1.75 < 2.5 < 3$ ; and sample points are  $c_1 = 0, c_2 = 0.5, c_3 = 1.75, c_1 = 2, c_2 = 3$  $1.75, c_4 = 2, c_5 = 3.$
- 10. (12 points) Evaluate the following definite integrals:

(a) 
$$\int_{1}^{1} (x+2)^{10} dx$$

(b) 
$$\int_{1}^{2} x^{3} dx$$

(c) 
$$\int_0^1 (4-x^2) dx$$
 (d)  $\int_0^1 \sqrt{x} dx$ 

## **Bonus (20 Points)**

- 11. (10 points) A homeowner has \$320 to spend on building a fence around a rectangular garden. Three sides of the fence will be constructed with wire fencing at a cost of \$ 2 per linear foot. The fourth side will be constructed with wood fencing at a cost of \$ 6 per linear foot. Find the dimensions and the area of the largest garden that can be enclosed with \$ 320 worth of fencing.
- 12. (10 points) Let f(x) = 2x on the interval [1, 2]. Calculate the left Riemann sum  $S_n$ , when partition the interval [1, 2] into n subintervals of equal length.